# UNIVERSITY EXAMINATIONS 2017/2018 ACADEMIC YEAR 

FOR THE DEGREE OF BACHELOR OF SCIENCE IN COMPUTER SCIENCE /APPLIED STATISTICS WITH COMPUTING SCHOOL: SCIENCE

COURSE CODE: MAT 110
COURSE TITLE: BASIC CULCULUS
DATE: $18^{\text {th }}$ December, 2017 TIME: $9.00 \mathrm{am}-12.00 \mathrm{pm}$
For examiner's Use Only

| Question | I.E | E.E |
| :--- | :--- | :--- |
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| CAT |  |  |
| EXAM |  |  |
| TOTAL |  |  |

INSTRUCTION TO CANDIDATES: SEE INSIDE
THIS PAPER CONSISTS OF 20 PRINTED PAGES
PLEASE TURN OVER
Insert the numbers of the questions you have answered in the order done
$\square$
Student Admission No.
.Exam Card No
Signature

## NSTRUCTION TO CANDIDATES

## Answer ALL questions from section A and any THREE from section B

 DO NOT WRITE ANYTHING ON THIS QUESTION PAPER
## SECTION A [31 Marks] ANSWER ALL QUESTIONS

## QUESTION ONE [16 marks]

a) Evaluate the following limits

> i.' $\quad \lim _{x \rightarrow 2} \frac{x^{2}-4}{x-2}[2 \mathrm{mks}]$
> ii.: $\quad \lim _{x \rightarrow \infty} \frac{2 x^{3}-3 x}{5 x^{3}+3}[2 \mathrm{mks}]$
b)
i. Define the term continuous

ij. Determine whether or not the function below is continuous at $\mathrm{x}=1$

$$
f(x)=\left\{\begin{array}{c}
\frac{x^{2}-1}{x-1} ; x \neq 1 \\
2 ; x=1
\end{array}[3 \mathrm{mks}]\right.
$$

c) Find the equation of the tangent and the normal to the curve $x^{2}+x y-y^{2}=1$ at the point $(2,3)$
d) A circular hole 10 cm in diameter and 30 cm deep metal is rebored to increase the diameter ${ }^{\text {to }}$ 10.3 cm . Estimate the amount of metal to be removed. Use MVT

## QUESTION TWO [15 marks]

a) Evaluate the integral $\int_{2}^{4}\left(x^{3}+2 x-7\right) d x$
b) The gradient function of a curve is given by $\frac{d x}{d y}=3 x^{2}+5$. Given t through the point $(1,8)$; determine the equation of the curve.
c) Differentiate the following with respect to x
i. $\quad y=\ln (\ln x)$
ii. $\quad y=\sin _{u}\left(2 x_{v}^{2}+3\right)$

Student Admission No
[3mks]
[4mks]
Signature
Exam Card

## INSTRUCTIONS TO CANDIDATES

1. Write your Admission Number, Exam Card Number and Sign in the spaces provided a bottom of each page of the Examination Booklet. DO NOT write your name anywhere in booklet.
2. Write on both sides of the pages.
3. All rough work must be done in the Answer sheets and crossed through.
4. If supplementary pages are used, they must be fastened all together at the end of this Booklet. Supplementary pages should be used only after all the leaves in the booklet have been exhausted.
5. It is a serious examination offence to cheat or to have unauthorized materials including MOBILE PHONES (whether on or off) in the examination venue.
6. In no circumstances must Answer Booklet used or unused, be removed from the examination room by a candidate.
7. The Booklet is for Examination use only in a designated examination room. Unauthorized possession of the Answer sheets by a student or any other person constitutes an examination irregularity calling for stiff disciplinary action.
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10. Candidates will not be allowed to leave the exam room once the exam commences.
11. Candidates are advised that importance is attached by examiners to accuracy and clarity of expression.
12. Committing any form of irregularity is prohibited and shall attract severe disciplinary action in accordance with Alupe University College Examination Regulations.
$\qquad$ Exam Card No. Signature.

## NSTRUCTION TO CANDIDATES

## Answer ALL questions from section $A$ and any THREE from section B DO NOT WRITE ANYTHING ON THIS QUESTION PAPER

## SECTION A [31 Marks] ANSWER ALL QUESTIONS

## QUESTION ONE [ 16 marks]

a) Evaluate the following limits

$$
\begin{aligned}
& \text { i.: } \quad \lim _{x \rightarrow 2} \frac{x^{2}-4}{x-2}[2 \mathrm{mks}] \\
& \text { ii.: } \quad \lim _{x \rightarrow \infty} \frac{2 x^{3}-3 x}{5 x^{3}+3}[2 \mathrm{mks}]
\end{aligned}
$$

b)

i. Define the term continuous
ij. Determine whether or not the function below is continuous at $\mathrm{x}=1$

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f(x)=\left\{\begin{array}{c}
\frac{x^{2}-1}{x-1} ; x \neq 1 \\
2 ; x=1
\end{array}[3 \mathrm{mks}]\right.
$$

c) Find the equation of the tangent and the normal to the curve $x^{2}+x y-y^{2}=1$ at the point $(2,3)$
d) A circular hole 10 cm in diameter and 30 cm deep metal is rebored to increase the diameter to 10.3 cm . Estimate the amount of metal to be removed. Use MVT

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a) Evaluate the integral $\int_{2}^{4}\left(x^{3}+2 x-7\right) d x$
[4mks]
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c) Differentiate the following with respect to x

$$
\begin{array}{ll}
\text { i. } & y=\ln (\ln x) \\
\text { ii. } & y=\sin \left(2 x_{v}^{2}+3\right)
\end{array}
$$

[3mks] [ 4 mks ]
Exam Card No. $\qquad$ Signature

