

**ALUPE UNIVERSITY
COLLEGE**
... Bastion of Knowledge...

P. O. Box 845-50400 Busia(K)
principal@auc.ac.ke
Tel: +254 741 217 185
+254 736 044 469
off Busia-Malaba road

**OFFICE OF THE DEPUTY PRINCIPAL
ACADEMICS, STUDENT AFFAIRS AND RESEARCH**

UNIVERSITY EXAMINATIONS

2020 /2021 ACADEMIC YEAR

FIRST YEAR SECOND SEMESTER REGULAR EXAMINATION

**FOR THE DEGREE OF BACHELOR OF
EDUCATION ARTS**

COURSE CODE: MAT 111
**COURSE TITLE: GEOMETRY AND ELEMENTARY
APPLIED MATHEMATICS**

DATE: TIME:

INSTRUCTION TO CANDIDATES

- SEE INSIDE

THIS PAPER CONSISTS OF 6 PRINTED PAGES

PLEASE TURN OVER

REGULAR – MAIN EXAM

MAT111: GEOMETRY AND ELEMENTARY APPLIED MATHEMATICS

STREAM: BSc (CS)

DURATION: 3 Hours

INSTRUCTION TO CANDIDATES

- i. Answer **ALL** questions from **section A** and any **THREE** from **section B**
- ii. Do not write on the question paper.

SECTION A (31 MARKS): ANSWER ALL QUESTIONS IN THIS SECTION.

QUESTION ONE[16MARKS]

- a) Find the distance between $A(2,-3)$ and the line $L : 3x - 4y + 2 = 0$ $L:3x - 4y + 2 = 0$. [4mks]
- b) Convert $2x - 5x^3 = 1 + xy$ into polar coordinates. [4mks]
- c) Find the distance between the points $P_1(3,-1,5), P_2(2,1,-1)$ [4mks]
- d) Find the distance from the point $(-1,2,1)$ to the line $(1,1,1) + t(2,3,-1)$. [4mks]

QUESTION TWO[15MARKS]

- a) Seagull can fly at a velocity of 9.00 m/s in still air. If
 - i. it takes the bird 20.0 min to travel 6.00 km straight into an oncoming wind, what is the velocity of the wind? [3mks]
 - ii. the bird turns around and flies with the wind, how long will it take the bird to return 6.00 km? [3mks]
- b) A car of mass 1.2tonnes is travelling along a straight horizontal road at a speed of $20ms^{-1}$ when it brakes sharply then skids. Friction brings the car to rest. If the coefficient of friction between the tyres and road is 0.8, calculate the:
 - i. deceleration. [3mks]
 - ii. distance travelled by the car before it comes to rest. [3mks]
- c) A particle A, of mass 2 kg, collides with a particle B, of mass 3kg. The velocity of particle A before the collision was $(4i - 3j)ms^{-1}$ and the velocity of particle B before the collision was $(4i + 4j)ms^{-1}$. Given the velocity of particle A after the collision was $(3i + 2j)ms^{-1}$, what was the velocity of B after the collision? [3mks]

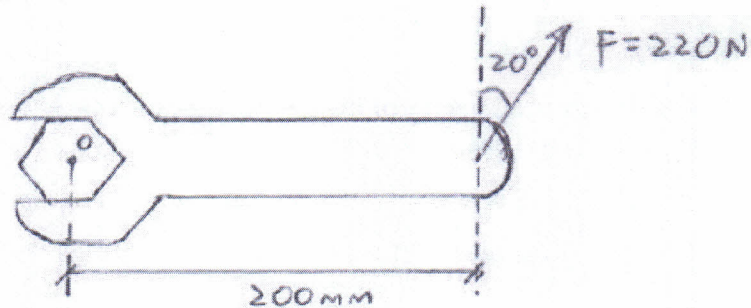
SECTION B:ANSWER ANY THREE QUESTIONS [39MARKS]

QUESTION THREE[13MARKS]

- a) Find the area of a triangle with vertices: $A(0,-3), B(5,0), C(0,3)$ [4mks]
- b) Convert $r = -8 \cos \theta$ into Cartesian coordinates [4mks]
- c) Find the standard equation of the sphere with center $(10,7,4), (-1,3,-2)$ [5mks]

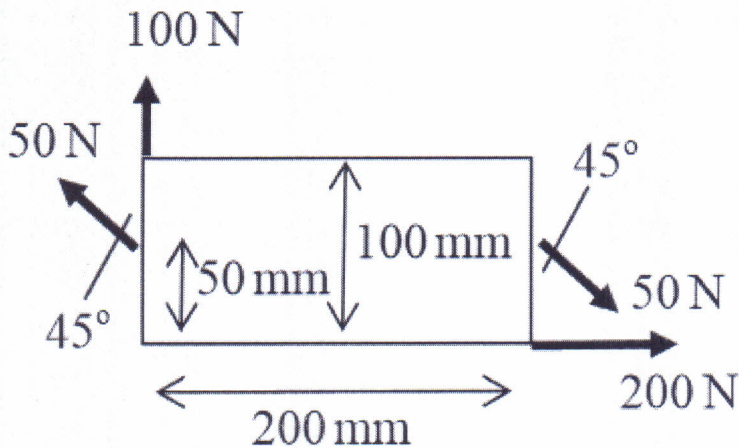
QUESTION FOUR[13MARKS]

- a) Find the distance from the point $(1,2,3)$ to the plane $2x - y + 3z = 5$ [5mks]
 b) Find the equivalent force -couple system about O. [8mks]



QUESTION FIVE[13MARKS]

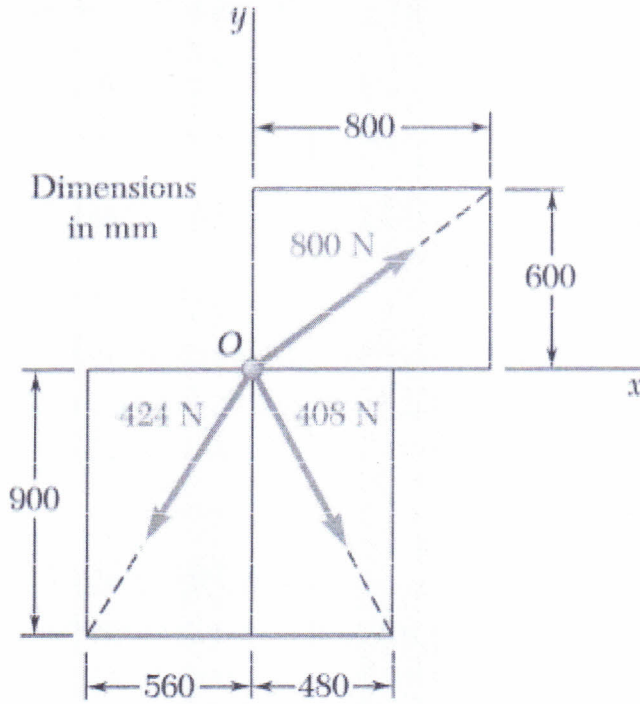
- a) Find the equation of the line passing through $(5,-1,3)$ having direction $\vec{v} = (1,0,-2)$. Express your answer in
- i. Symmetric form [1mk]
 - ii. Vector form [2mks]
 - iii. Parametric form [2mks]
 - iv. Find two other points on the line [2mks]
- b) Consider the plate subjected to the four external loads shown in the figures below. An equivalent force-couple system F-M, with the force acting at the centre of the plate, can be calculated through? [6mks]



QUESTION SIX[13MARKS]

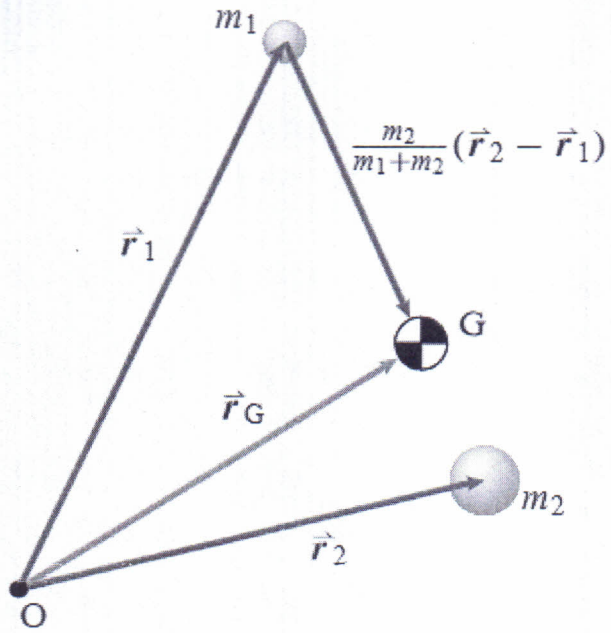
a) Determine the x, y components of the 3 forces.

[8mks]



b) Derive an equation for center of mass r_{CM} of a system consisting of two points as shown below.

[5mks]



QUESTION SEVEN[13MARKS]

- a) A pitcher tosses a baseball straight up, with an initial speed of 25 m/s.
- i. How long does it take to reach its highest point? [3mks]
 - ii. How high does the ball rise above its release point? [3mks]
 - iii. How long will it take for the ball to reach a point 25 m above its release point. [3mks]
- b) For the 45° position of the pump handle with force P perpendicular to the handle, determine graphically the angle θ between the handle and the compensating link AB which enables the force transmitted to the plunger to be along its vertical axis. [4mks]

